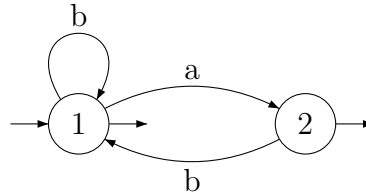
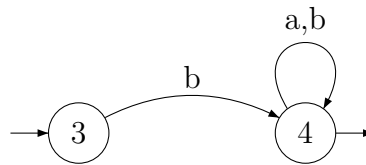


Here is one acceptor, A . The language of this acceptor $L(A)$ is equal to the set containing all and only those strings which do not have consecutive a symbols.



Here is another acceptor, B . The language of this acceptor $L(B)$ is equal to the set containing all and only those strings which begin with the b symbols.



Now we will compute the product using the definition.

$$Q = \{(1, 3), (1, 4), (2, 3), (2, 4)\}$$

$$I = \{(1, 3)\}$$

$$F = \{(1, 4), (2, 4)\}$$

$$\delta((1, 3), b) = (1, 4) \text{ since } \delta_A(1, b) = 1 \text{ and } \delta_B(3, b) = 4.$$

$$\delta((1, 4), b) = (1, 4) \text{ since } \delta_A(1, b) = 1 \text{ and } \delta_B(4, b) = 4.$$

$$\delta((2, 3), b) = (1, 4) \text{ since } \delta_A(2, b) = 1 \text{ and } \delta_B(3, b) = 4.$$

$$\delta((2, 4), b) = (1, 4) \text{ since } \delta_A(2, b) = 1 \text{ and } \delta_B(4, b) = 4.$$

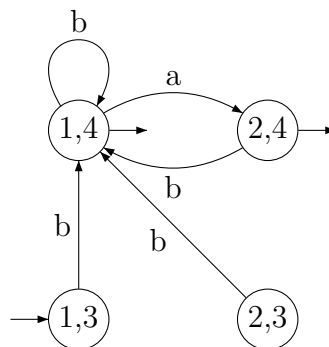
$$\delta((1, 3), a) \text{ does not exist because } \delta_B(3, a) \text{ does not exist.}$$

$$\delta((1, 4), a) = (2, 4) \text{ since } \delta_A(1, a) = 2 \text{ and } \delta_B(4, a) = 4.$$

$$\delta((2, 3), a) \text{ does not exist because neither } \delta_A(2, a) \text{ nor } \delta_B(3, a) \text{ exists.}$$

$$\delta((2, 4), a) \text{ does not exist since } \delta_A(2, a) \text{ does not exist.}$$

Pictorially, $A \times B$ looks like this. Note that $L(A \times B) = L(A) \cap L(B)$.



Is state $(2,3)$ a useful state?